

Summary of Hypothesis Tests

Test	Parameter	Null Hypothesis ²	Test Statistic ³	Assumptions ⁴	<i>R</i>
one-proportion <i>z</i> -test	proportion (p)	$H_0 : p = p_0$	$z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$	at least 15 expected successes and 15 expected failures under H_0	<i>prop.test</i>
one-sample <i>t</i> -test	mean (μ)	$H_0 : \mu = \mu_0$	$t = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$, df = $n - 1$	$n \geq 30$ or observations are from a normal distribution	<i>t.test</i>
two-proportion <i>z</i> -test	Difference in proportions ($p_1 - p_2$)	$H_0 : p_1 - p_2 = 0$	$z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{p(1-p)\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}$, and $p = \frac{n_1\hat{p}_1 + n_2\hat{p}_2}{n_1 + n_2}$.	independent samples, at least 15 expected successes and 15 expected failures under H_0	<i>prop.test</i>
two-sample <i>t</i> -test	Difference in means ($\mu_1 - \mu_2$)	$H_0 : \mu_1 - \mu_2 = 0$	$t = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$, df by Satterthwaite formula	independent samples with unequal variances, there are at least 30 observations for each group or observations are from a normal distribution	<i>t.test</i>

²The alternative hypothesis H_A is obtained by replacing '=' with \neq (two-tailed alternative). One-tailed alternative hypotheses are not discussed and are not recommended.

³See table below

⁴All analyses assume that the observations come from a random process (i.e., a random sample or an experiment where the treatment is randomly assigned)

³ Test statistic	Description
z	follows the standard normal distribution under H_0
t	follows the t distribution with given degrees of freedom under H_0