# Analysis of Algorithms: <br> Data Cleanup Algorithms 

Garrett Dancik, PhD<br>Fall 2021

Course Notes: https://gdancik.github.io

## What do we mean by Data Cleanup?

- If data contains invalid or missing values, those invalid values should be removed.
- In a survey, a student does not enter their age (or enters an invalid one)
- In a survey, a student does not enter their GPA (or enters an invalid one)
- We will assume that missing / invalid values are recorded as 0
- Example data:

| 0 | 21 | 19 | 0 | 18 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- |

- In this case, we want a list containing only the numbers: $21,19,18$, and 19


## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1



## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1



## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1



## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., -1 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1


Original list


## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1


Since the first number is 0 , we shift all other numbers one position to the left

## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1


Since the first number is 0 , we shift all other numbers one position to the left

## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1


Since the first number is 0 , we shift all other numbers one position to the left

## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1


Since the first number is 0 , we shift all other numbers one position to the left

## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1

| 0 | 21 | 19 | 0 | 18 | 19 | Original list |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | num_valid $=5$ |  |  |  |  |  |
| 21 | 19 | 0 | 18 | 19 | 19 | Updated list |

## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1



## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1


21


## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1


## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1


| 21 | 19 | 0 | 18 | 19 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- |

## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1


| 21 | 19 | 18 | 18 | 19 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- |

## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1


| 21 | 19 | 18 | 19 | 19 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- |

## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1



## Shuffle-left algorithm

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1
- The final list, containing 4 valid items, is below:



## Shuffle-left algorithm:

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1
- Running time (best case)
- If no numbers are invalid, then the while loop is executed $n$ times, where $n$ is the initial size of the list, and the only other operations are the comparison in the if statement, and position is increased by 1 . The running time is $\theta(n)$. This is the best case.


## Shuffle-left algorithm:

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1
- Running time (worst case):
- If all the numbers are invalid, then for all $n$ passes through the list, $\mathrm{n}-1$ copies (shifts) are made. This is a worst case.
- The total number of operations in the loop is (ignoring comparisons):
- For the first position: $\mathrm{n}+1$ operations: $\mathrm{n}-1$ copies, plus 2 to increase num_valid and position
- For the second position: n operations, $\mathrm{n}-2$ copies, plus 2 to increase num_valid and position
- The total number of operations is the sum of 1 through $\mathrm{n}+1$ which equals
- $\mathrm{n}(\mathrm{n}+1) / 2+1 \rightarrow \theta\left(n^{2}\right)$


## Shuffle-left algorithm:

- While position <= num_valid :
- If num[position] is invalid, e.g., 0 :
- All valid numbers to the right of num are shifted 1 position to the left
- Decrease num_valid by 1
- Else:
- Increase position by 1
- Running time:
- Best case (all entries are valid) is $\theta(n)$
- Worst case (all entries are invalid) is $\theta\left(n^{2}\right)$
- Average case is also $\theta\left(n^{2}\right)$
- Space:
- $n$ (all cases - best, worst, and average) ( $n$ is required for the original list, plus a few additional variables)


## Copy-over algorithm

- Find the total number of valid elements in the list, and store in num_valid
- Create an empty list, called copyNum, of length num_valid
- Set index to 0
- For each num in the original list:
- If num is valid
- Assign num to copyNum[index]
- Increase index by 1

| 0 | 21 | 19 | 0 | 18 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- |

## Copy-over algorithm

- Find the total number of valid elements in the list, and store in num_valid
- Create an empty list, called copyNum, of length num_valid
- Set index to 0
- For each num in the original list:
- If num is valid
- Assign num to copyNum[index]
- Increase index by 1

| 0 | 21 | 19 | 0 | 18 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- |



## Copy-over algorithm

- Find the total number of valid elements in the list, and store in num_valid
- Create an empty list, called copyNum, of length num_valid
- Set index to 0
- For each num in the original list:
- If num is valid
- Assign num to copyNum[index]
- Increase index by 1

| 0 | 21 | 19 | 0 | 18 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- |

x


```
Index = 0
```


## Copy-over algorithm

- Find the total number of valid elements in the list, and store in num_valid
- Create an empty list, called copyNum, of length num_valid
- Set index to 0
- For each num in the original list:
- If num is valid
- Assign num to copyNum[index]
- Increase index by 1



## Copy-over algorithm

- Find the total number of valid elements in the list, and store in num_valid
- Create an empty list, called copyNum, of length num_valid
- Set index to 0
- For each num in the original list:
- If num is valid
- Assign num to copyNum[index]
- Increase index by 1


```
Index = 2
```


## Copy-over algorithm

- Find the total number of valid elements in the list, and store in num_valid
- Create an empty list, called copyNum, of length num_valid
- Set index to 0
- For each num in the original list:
- If num is valid
- Assign num to copyNum[index]
- Increase index by 1

| 0 | 21 | 19 | 0 | 18 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- |

X

| 21 | - | num_valid $=4$ |
| :--- | :--- | :--- | :--- |

```
Index=2
```


## Copy-over algorithm

- Find the total number of valid elements in the list, and store in num_valid
- Create an empty list, called copyNum, of length num_valid
- Set index to 0
- For each num in the original list:
- If num is valid
- Assign num to copyNum[index]
- Increase index by 1



## Copy-over algorithm

- Find the total number of valid elements in the list, and store in num_valid
- Create an empty list, called copyNum, of length num_valid
- Set index to 0
- For each num in the original list:
- If num is valid
- Assign num to copyNum[index]
- Increase index by 1


```
Index = 4
```


## Copy-over algorithm

- Find the total number of valid elements in the list, and store in num_valid
- Create an empty list, called copyNum, of length num_valid
- Set index to 0
- For each num in the original list:
- If num is valid
- Assign num to copyNum[index]
- Increase index by 1


## - Running time:

- The first step is order $n$, since we need to iterate through all elements in the list to count the number of valid elements. For each element, there is a constant number of operations. (More details for this step are required, but this likely would use a for loop).
- The main work then occurs in the for loop on the $4^{\text {th }}$ line, which is also order $n$. For each element, we either copy it or not, and this is also a constant number of operations for each of the $n$ elements.
- The running time is $\theta(n)$, in the best, worst, and average cases.


## Copy-over algorithm

- Find the total number of valid elements in the list, and store in num_valid
- Create an empty list, called copyNum, of length num_valid
- Set index to 0
- For each num in the original list:
- If num is valid
- Assign num to copyNum[index]
- Increase index by 1
- Space (depends on the number of valid elements):
- Best case: if there are no valid elements, then the space only requires the original list, which is $n$ (we ignore a few additional variables)
- Worst case: if all the elements are valid, we create an additional copy of the original list. The space requirements are $2 n$.
- Average case: this depends on the expected number of valid/invalid items, and will be between $n$ and $2 n$. If the number of valid items is equally likely to be between $0,1,2, \ldots n$, then the average space requirement is $1.5 n$.


## Converging pointers algorithm

- We keep a left and right index
- Set left to 0 and right to $n-1$ (index of the last element)
- Set num_valid to the length of the numbers list
- While left < right
- If number[left] is valid :
- Increase left by 1
- Else (number[left] is not valid) :
- Copy number[right] to number[left]
- Decrease num_valid by 1
- Decrease right by 1
- If number[left] is not valid :

- Decrease num_valid by 1


## Converging pointers example


num_valid $=6$

Item at left is 0 , so we copy from right to left, and decrease right and num_valid by 1.

## Converging pointers example


num_valid = 5

Item at left is not 0 , so we increase left by 1

## Converging pointers example


num_valid = 5

Item at left is not 0 , so we increase left by 1

## Converging pointers example



Item at left is not 0 , so we increase left by 1

## Converging pointers example



Item at left is 0 , so we copy from right to left, and decrease right and num_valid by 1.

## Converging pointers example


num_valid $=4$

Item at left is not 0 (if it was, we would decrease num_valid).
Once left is equal to right, we are done

## Converging pointers algorithm

- While left < right
- If number[left] is valid:
- Increase left by 1
- Else (number[left] is not valid) :
- Copy number[right] to number[left]
- Decrease num_valid by 1
- Decrease right by 1
- If number[left] is not valid:
- Decrease num_valid by 1
$\longleftarrow \quad$ Correction: this is after the while loop.
- Running time:
- The main work occurs in the while loop. The loop always increases left or decreases right, until left and right are the same. This can only happen $n$ times. All other operations inside the loop are constant, so the running time is $\theta(n)$, which is true for the best, worst, and average cases.
- Space: $n$ (we need space only for the original list, as well as a few additional terms). This is the most space efficient algorithm


## Data Cleanup Algorithms

|  | Shuffle-left |  | Copy over |  | Converging Pointers |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Time | Space | Time | Space | Time | Space |
| Best | $\theta(n)$ | $n$ | $\theta(n)$ | $n$ | $\theta(n)$ | $n$ |
| Worst | $\theta\left(n^{2}\right)$ | $n$ | $\theta(n)$ | $2 n$ | $\theta(n)$ | $n$ |
| Average | $\theta\left(n^{2}\right)$ | $n$ | $\theta(n)$ | $(n, 2 n)$ | $\theta(n)$ | $n$ |

- Which algorithm is the best?

